



INSTITUTE FOR RESEARCH IN  
**ELECTRONICS**  
& **APPLIED PHYSICS**



# 3D Imaging of Segregation in Granular Shear Flows

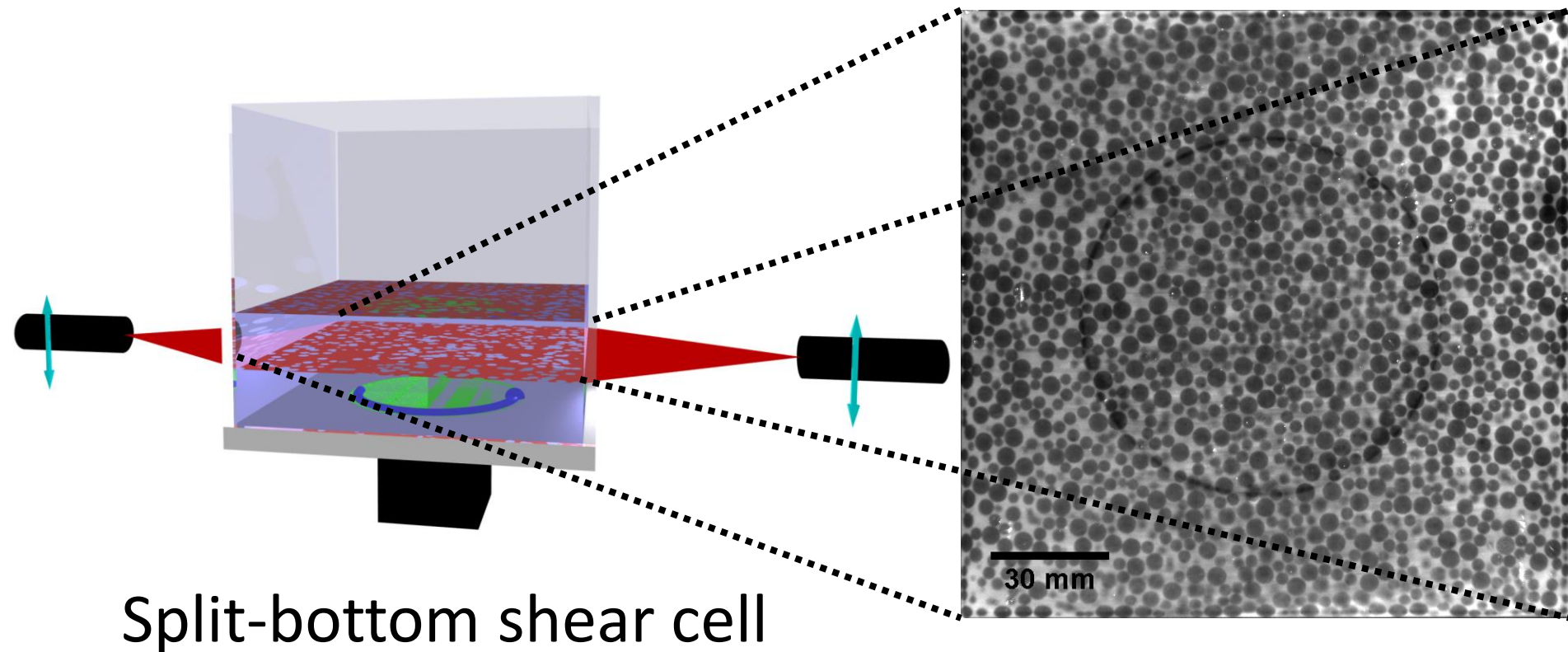
Matt Harrington<sup>1</sup>, Joost H. Weijs<sup>2</sup>, and Wolfgang Losert<sup>1</sup>

<sup>1</sup>University of Maryland

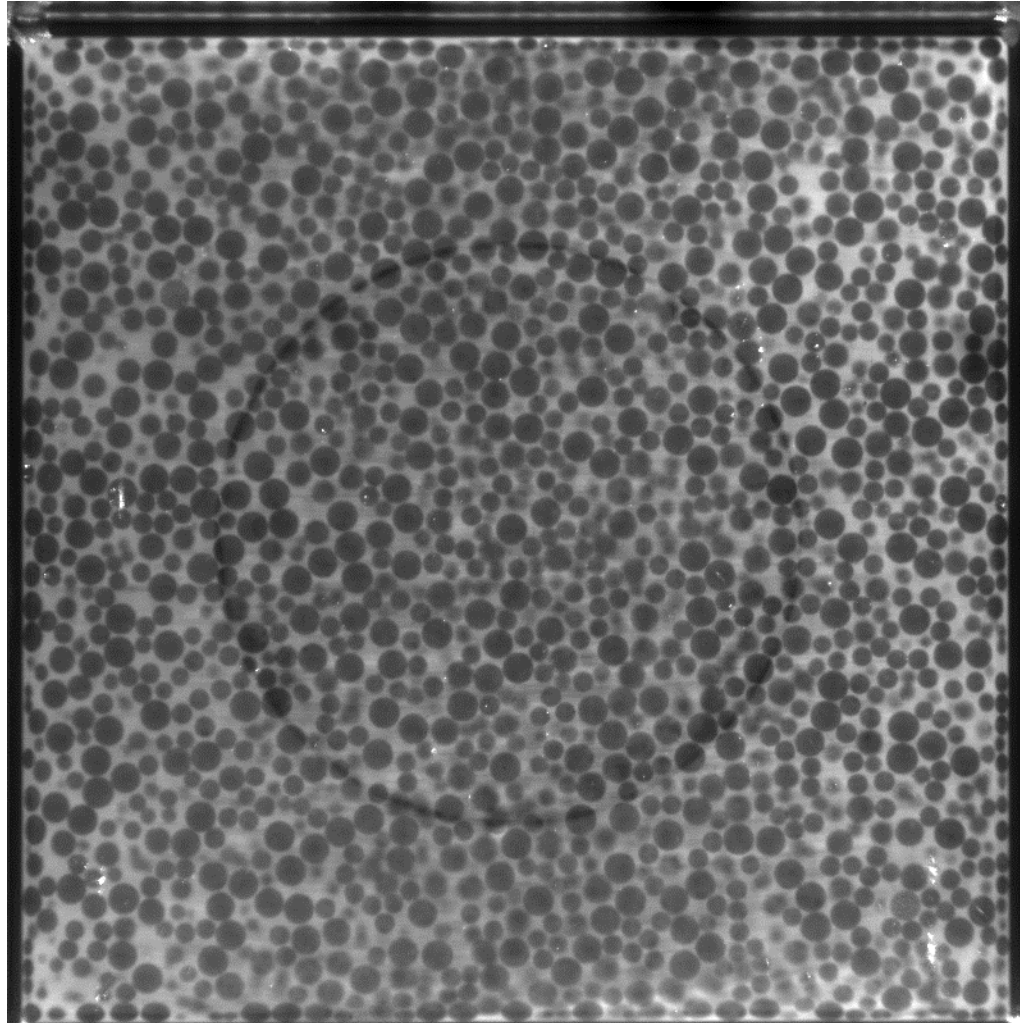
<sup>2</sup>University of Twente

# Refractive Index Matched Scanning (RIMS)

Invited Review: Dijksman, et al, *Rev. Sci. Instr.* 2012

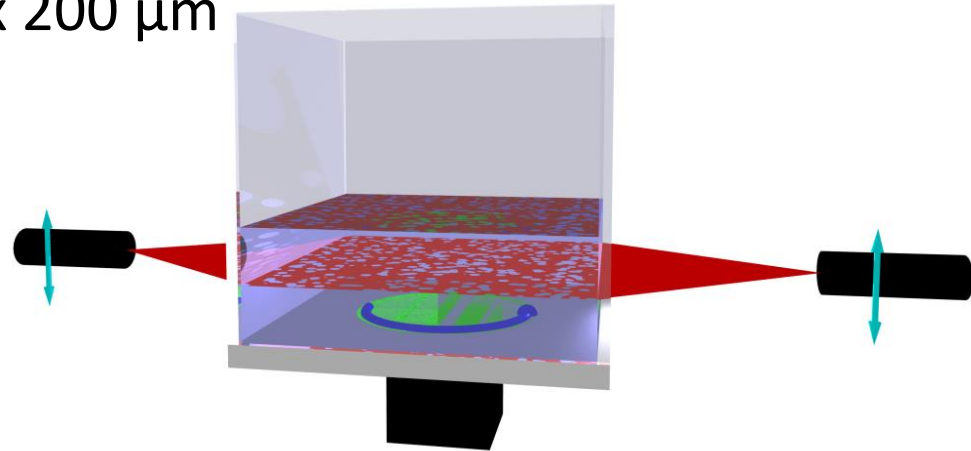


# Flythrough



# Parameters:

- Quasi-static shear rate  $\Omega = 0.001$  rad/s (Dijksman, et al, *PRE* 2010)
- Shear is performed in  $2^\circ$  (0.035 radian) steps
- $R_s = 45$  mm,  $L = 150$  mm
- 1 voxel  $\approx 200 \mu\text{m} \times 200 \mu\text{m} \times 200 \mu\text{m}$



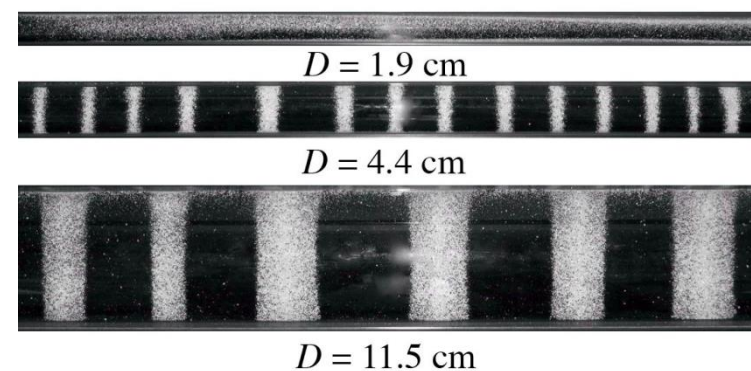
# Procedure:

- Capture images after each shear increment
- Convolution kernel gives 3D particle center locations (Tsai and Gollub, *PRE* 2004)
- Particle center resolution of  $\sim 100 \mu\text{m}$
- Lagrangian Particle Tracking (Ouellette, et al, *Exp. Fluids* 2006)

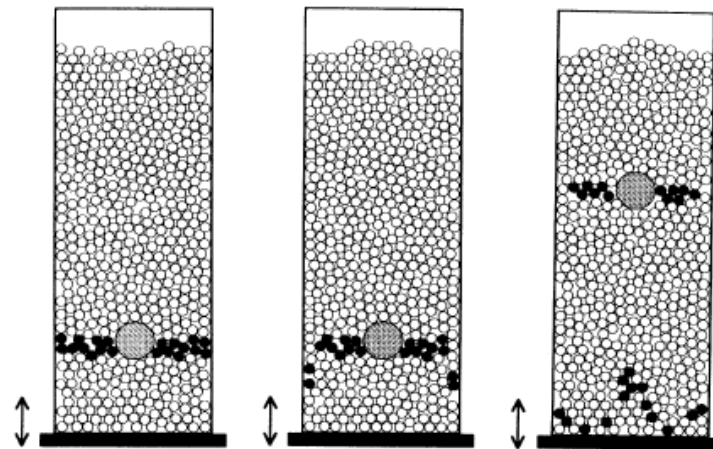


# Segregation: definition and examples

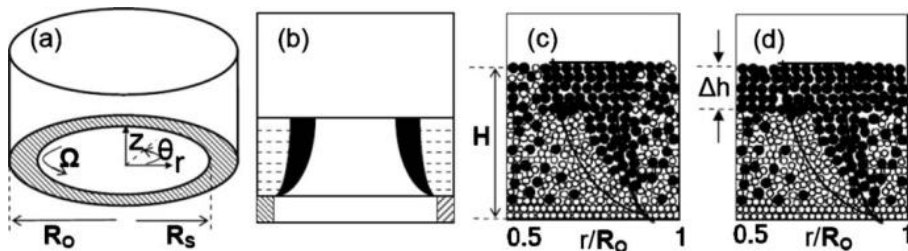
**Segregation** is the separation of granular mixtures by physical property (e.g., size, density) under a driving force



Charles, et al, *Gran. Matt.* 2006



Knight, et al, *PRL* 1993



Fan & Hill, *PRE* 2010



H. A. Makse

# What we don't (and would like to) know

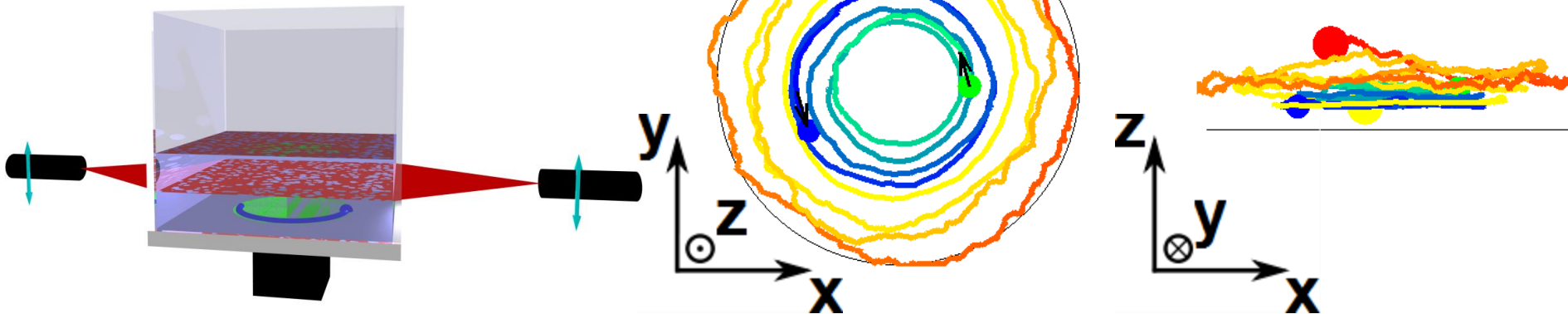
Consistent, robust predictive model for shear-driven segregation of a dense 3D granular material

## **What do we need?**

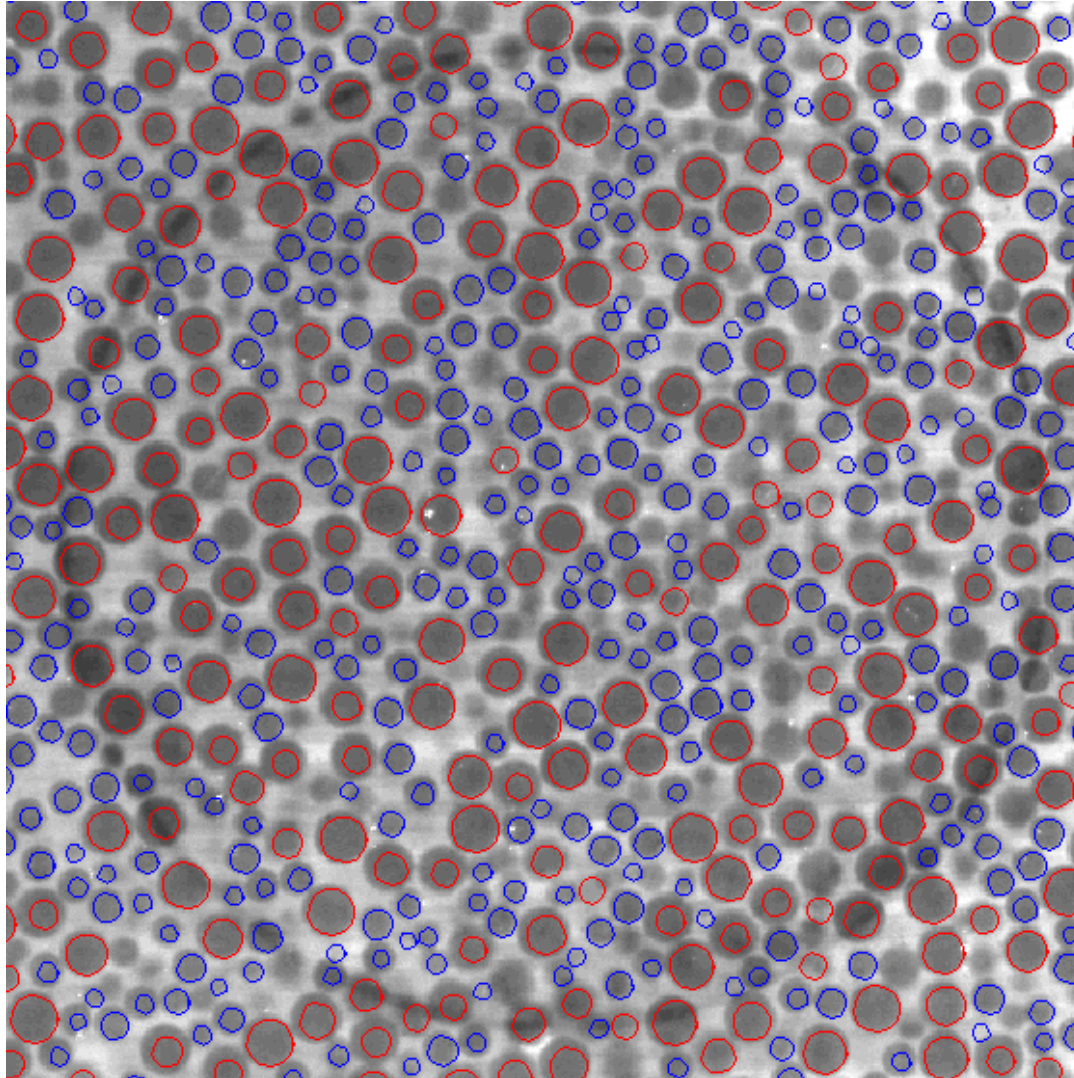
- Account for seemingly inconsistent experimental results
- Absolute particle size effects – segregation length scale?
- Particle-scale dynamics?
- Internal dynamics/flows?

# Bidisperse setup

- PMMA (acrylic) spheres: Refractive index  $n = 1.49$   
 $D_S = 1/8$  inch (3.2 mm) and  $D_L = 3/16$  inch (4.8 mm)  
 $\hookrightarrow 3 D_S = 2 D_L$
- Index-matched fluid: Triton X-100 with Nile Blue 690 Perchlorate
- Twin laser sheets with  $\lambda = 635$  nm
- $27 M_S = 16 M_L \leftrightarrow N_S = 2 N_L$
- $H = 46$  mm  $\approx 10 D_L \approx R_s$



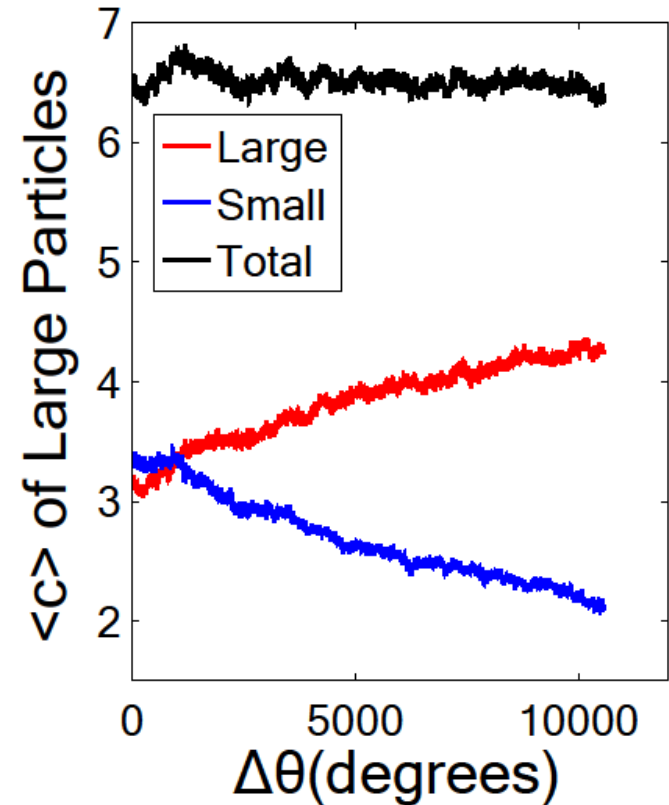
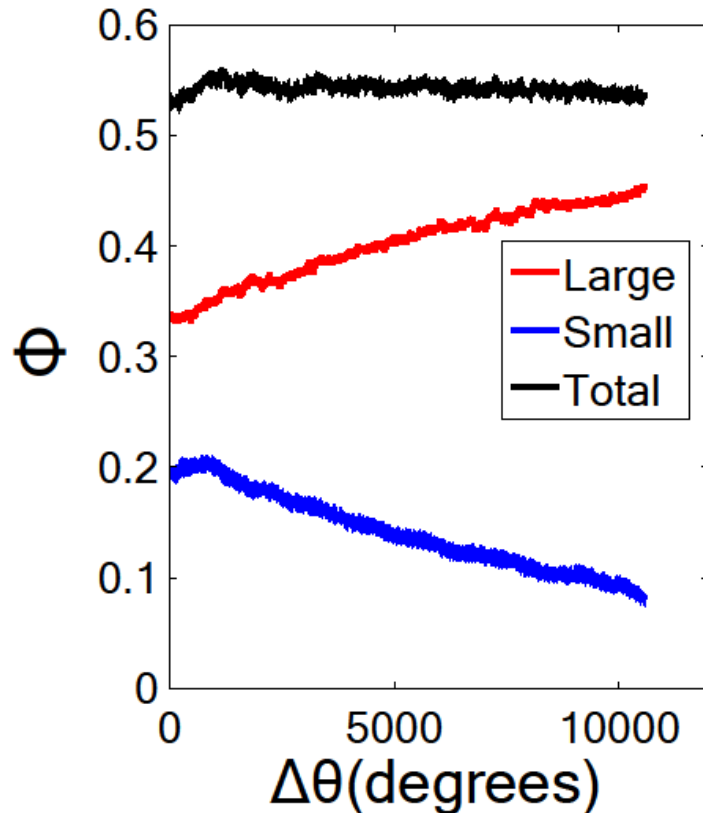
# Steady shear at $z = 3.8 \text{ cm}$ ( $8 D_L$ )





# Segregation under steady shear

## Global and local phenomenon

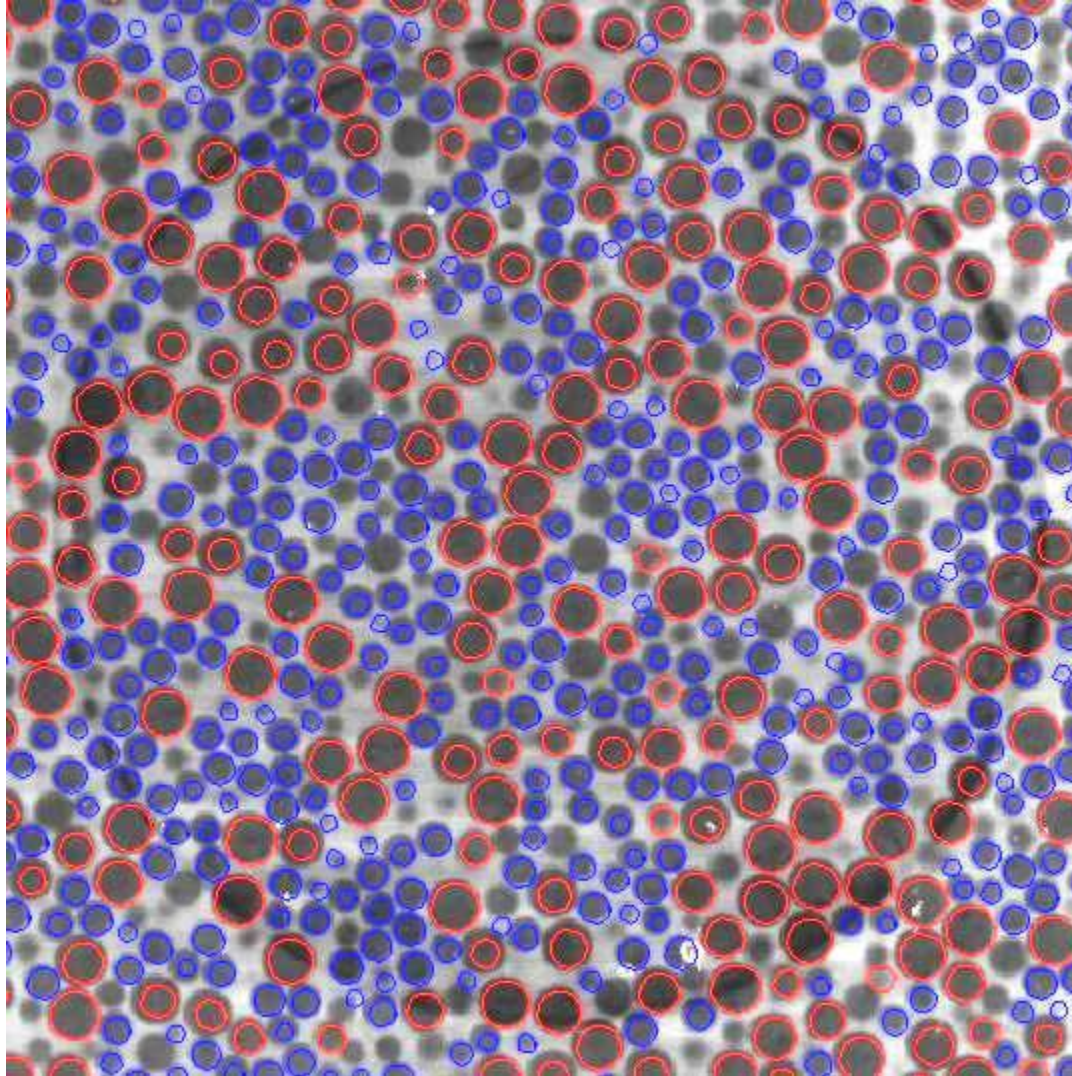


Volume fraction -- **GLOBAL**      Average coordination number -- **LOCAL**

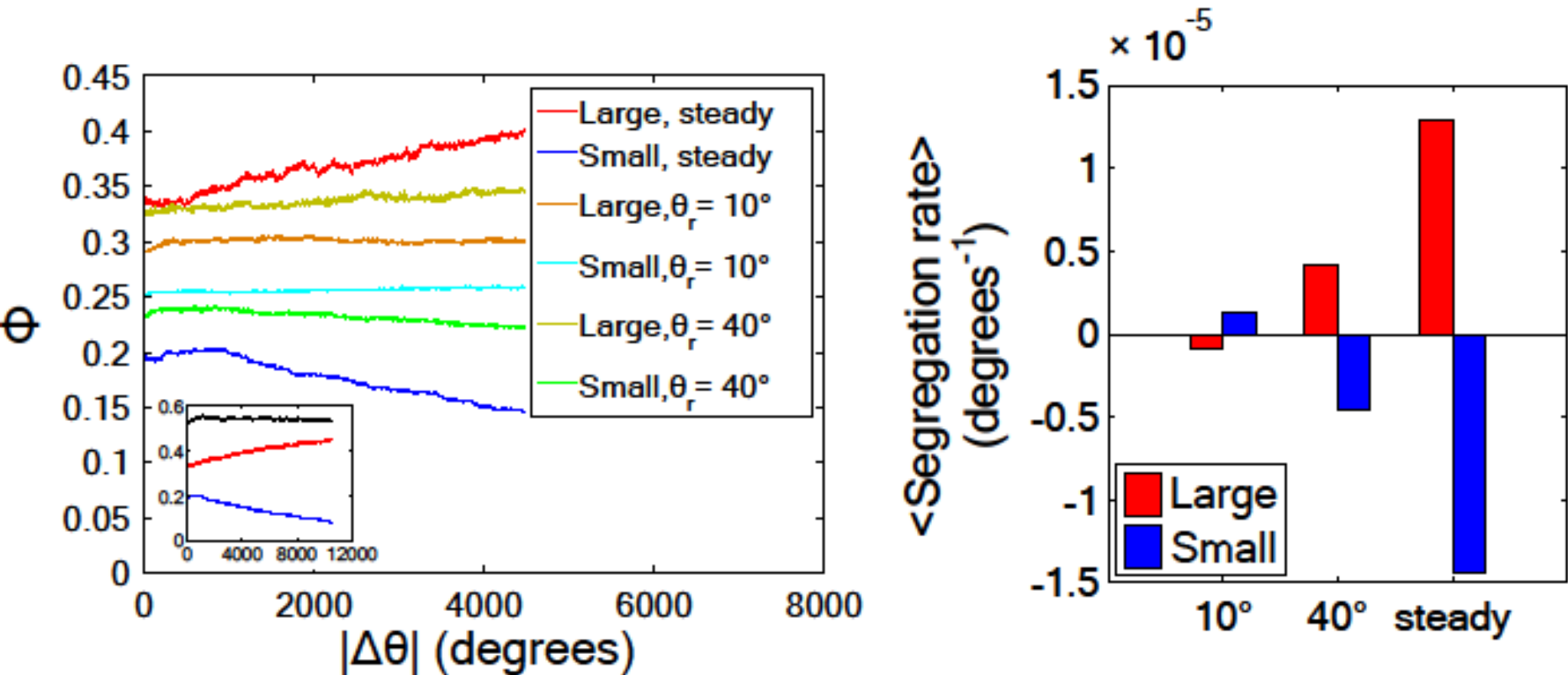
$$\phi = \frac{V_{parts}}{V_{space}}$$

$$\langle c \rangle = \text{Average number of large/small contacts}$$

10° cyclic shear at  $z = 3.8$  cm ( $8 D_L$ )

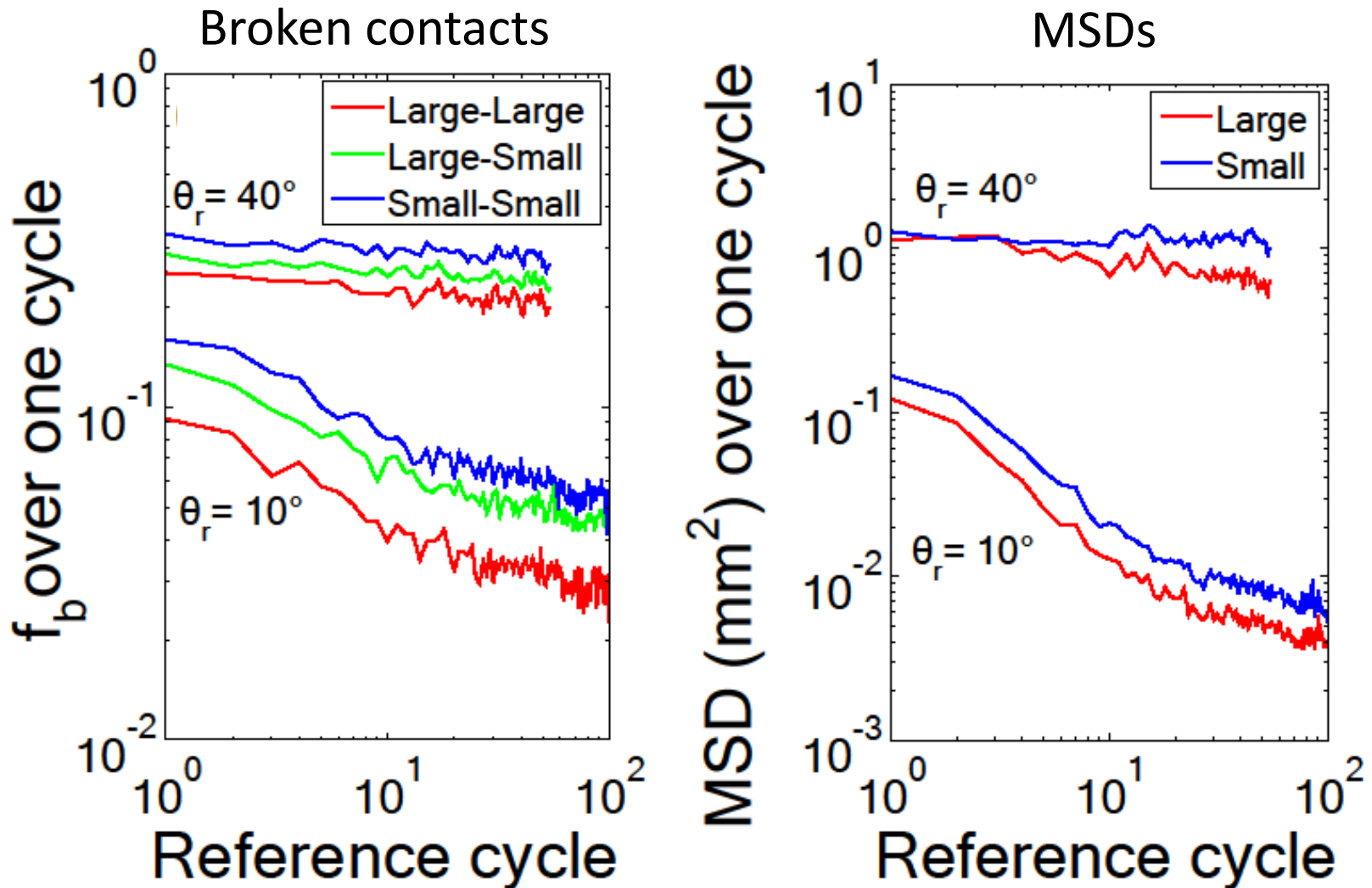


# Segregation under cyclic shear?



There appears to be a segregation transition between  $10^\circ$  and  $40^\circ$  cyclic shear

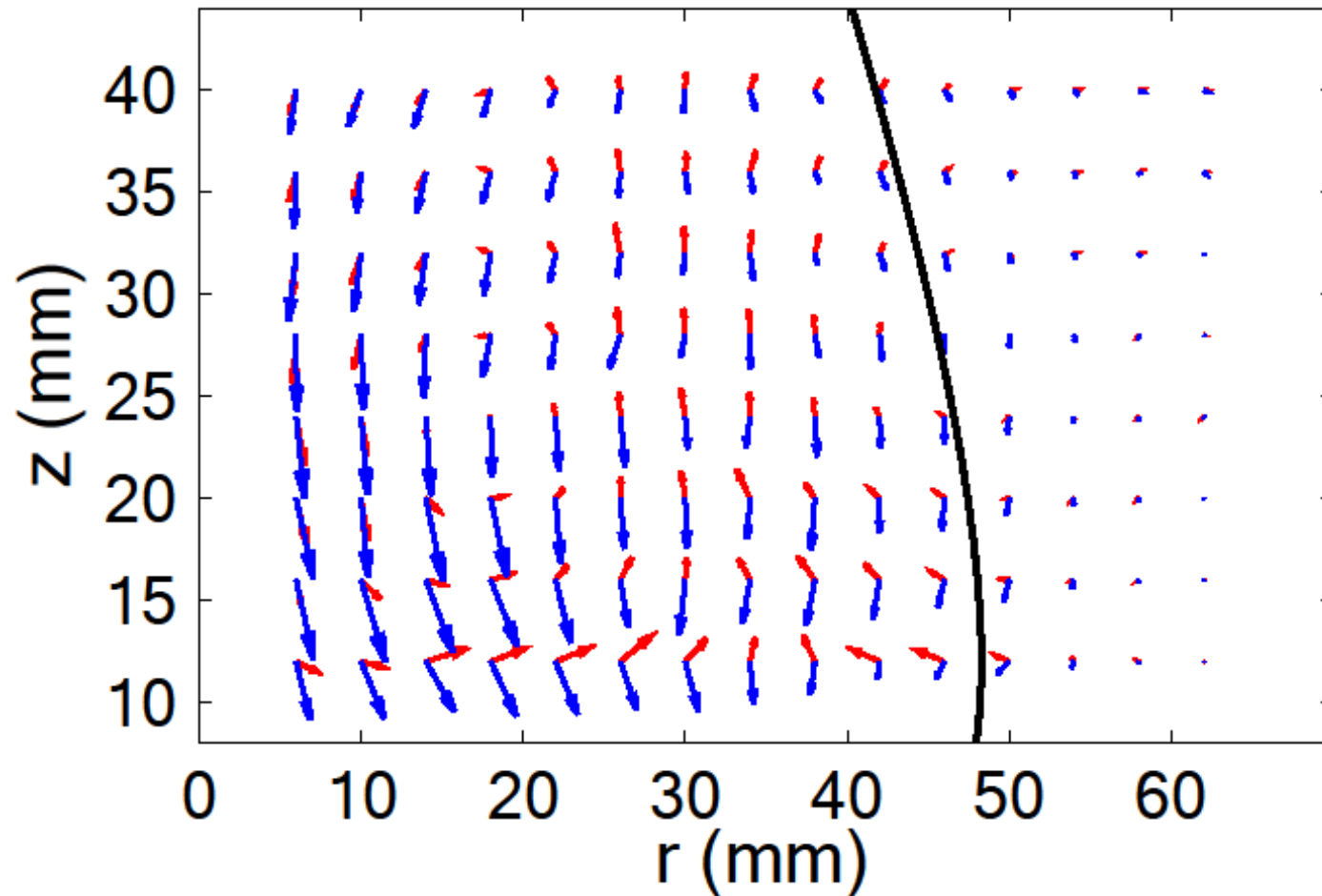
# Microscale Reversibility



Similar trends for  $D_L$  monodisperse system (Slotterback, et al, *PRE* 2012)

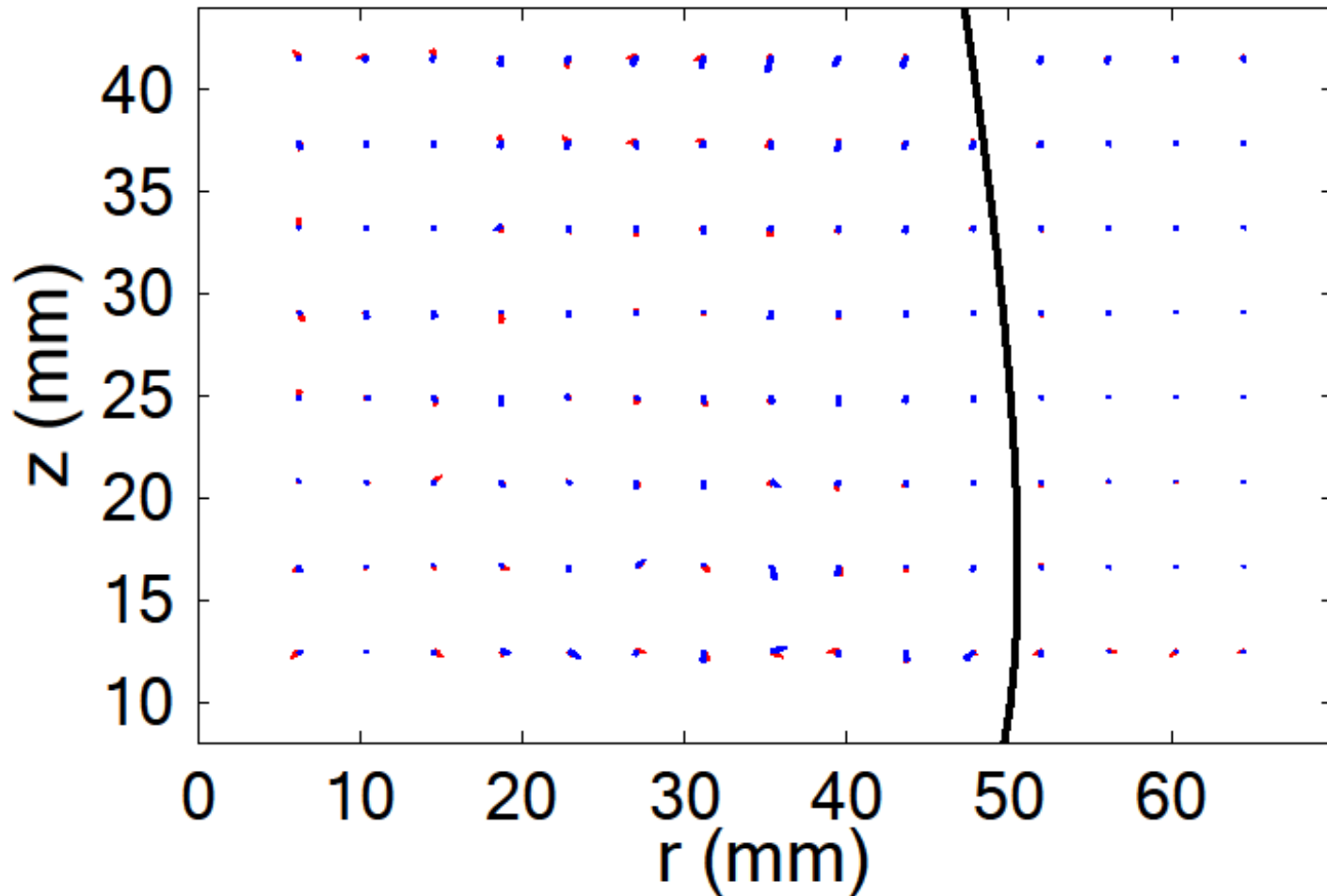


# Secondary flows – steady shear



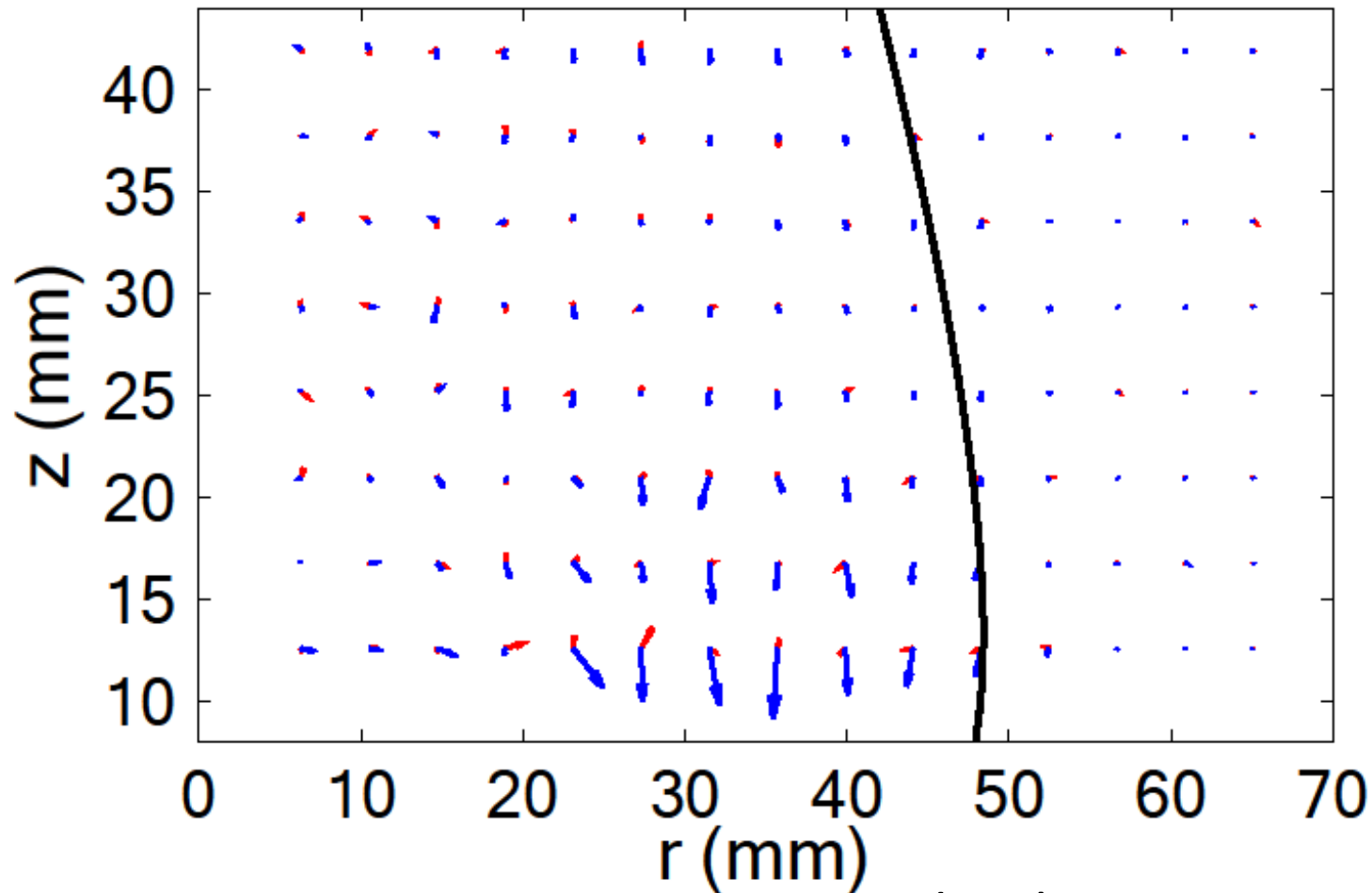
Convection of large grains  
Net downward flux of small grains

# Secondary flows – $\theta_r = 10^\circ$



Very diminished magnitude of flows

# Secondary flows – $\theta_r = 40^\circ$



Convection starts to develop

Downward drift of small grains near disk

# Summary

- Critical strain amplitude for segregation under cyclic shear
  - Continuum gradient-based models are not enough!
- Bulk segregation concurrent with microscale irreversibility
- Amplitude-dependent secondary flows:
  - Convection of large grains
  - Downward drift of small grains



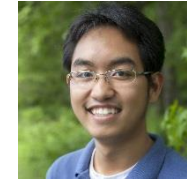
***Principal Investigator:*** Wolfgang Losert



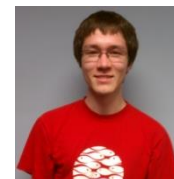
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Kerstin Nordstrom



***Graduate Students:*** Matt Harrington  
Mark Herrera  
Steve Slotterback



***Undergraduate Student:*** Michael Lin



***Visiting Student:*** Joost Weijs (U. Twente)

