Numerical Simulations Studying Size Segregation in a Rotating Drum

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### Motivation

Investigate the effect on granular flow of a distribution of particle sizes inside the bed thereby, investigate how well theories and correlations developed for mono-dispersed perform for more complex poly-disperse systems



# Granular Flows

- **Particulate materials exist in many industries including** metallurgical, chemical, food, pharmaceuticals, ceramic
- It is sometimes preferable to separate components from mixture whereas, sometimes mixing produces the final product
- Rotary drum is often used as granular mixer, gas/solid reactor, dryer





- **Focus on rolling regime which is common for mixing** purposes
- Granular bed in rolling mode can divided into two distinct regions:
	- $\blacktriangleright$  Thin active layer
	- $\blacktriangleright$ **Larger passive layer**



Source: Alizadeh et al.,AIChE J., 59(6), 2013



Radioactive tracing was used to collect data in plexi-glass drum





Composition of poly-disperse systems was chosen to ensure rapid segregation





- $\begin{array}{c} \hline \end{array}$ **Particle density,**  $\rho_s = 2500kg/m^3$
- $\begin{array}{c} \hline \end{array}$ **Gas density,**  $\rho_{g} = 1.18 kg/m^{3}$
- $\blacktriangleright$ **Gas viscosity,**  $\mu_{g} = 1.8 \times 10^{-5} Pa.s$
- Ь ▶ Drum diameter,  $D = 24$ *cm*
- $\blacktriangleright$ ▶ Drum Length, L=36cm
- $\blacktriangleright$ Bed height, 35 % *of volume*





# Model setup in STAR -CCM+

- $\blacktriangleright$ Algebraic model for granular temperature
- $\begin{array}{c} \hline \end{array}$ Fluid particle drag modelled using Gidaspow drag
- $\blacktriangleright$  $\blacktriangleright$   $\;$  Inter-particle drag modelled using Gera-Syamlal drag
- $\blacktriangleright$ Particle kinetic viscosity modelled using Gidaspow model
- $\blacktriangleright$ Frictional regime modelled using Schaeffer model
- $\blacktriangleright$  $\blacktriangleright$  Coefficient of restitution,  $e$  =  $0.9$
- $\blacktriangleright$ Maximum particle volume fraction set at 0.624



# Governing Equations

▶ Continuity

$$
\frac{\partial}{\partial t} \alpha_k \rho_k + \nabla \bullet \alpha_k \rho_k u_k = 0
$$

Fluid Momentum

$$
\frac{\partial}{\partial t} \alpha_k \rho_k u_k + \nabla \bullet \alpha_k \rho_k u_k u_k = -\alpha_k \nabla p + \alpha_k \rho_k g + \nabla \bullet \alpha_k \tau_k + F_I
$$

▶ Solid Momentum

$$
\frac{\partial}{\partial t}\alpha_s \rho_s u_s + \nabla \bullet \alpha_s \rho_s u_s u_s = -\alpha_s \nabla p - \nabla p_s + \alpha_s \rho_s g + \nabla \bullet \alpha_s \tau_s + F_I
$$



# Granular Temperature formulation

 $\pi$ 

*s*

*d*

 $\blacktriangleright$  Granular temperature is calculated by an algebraic relation derived by assuming local equilibrium between production and dissipation of fluctuating energy.

$$
\sqrt{\theta} = \begin{cases}\n-\frac{K_1 \varepsilon_s D_{ii} + \sqrt{K_1^2 D_{ii}^2 \varepsilon_s^2 + 4K_4 \varepsilon_s \left[K_2 D_{ii}^2 + 2K_3 D_{ij} D_{ij}\right]}}{2\varepsilon_s K_4}\n\end{cases}
$$
\n
$$
K_1 = 2\rho_s g_0 (1 + e)
$$
\n
$$
K_2 = \frac{4d_s \rho_s \varepsilon_s g_0 (1 + e)}{3\sqrt{\pi}} - \frac{2}{3} K_3
$$
\n
$$
K_3 = \frac{\rho_s d_s}{2} \left\{ \frac{\sqrt{\pi}}{3(3 - e)} [0.5(3e + 1) + 0.4(1 + e)(3e - 1)\varepsilon_s g_0] + \frac{8\varepsilon_s g_0 (1 + e)}{5\sqrt{\pi}} \right\}
$$
\nParticle diameter

\n
$$
K_4 = \frac{12(1 - e^2)\rho_s g_0}{1/\sqrt{\rho_s}} \qquad \qquad \text{Particle density} \qquad \rho_s
$$

Particle density 
$$
\rho_s
$$

\nStrain rate tensor  $D_{ij}$ 



### Kinetic theory stress tensor

$$
S_{s} = \left[ -P_{s} + \left( \xi_{s} - \frac{2}{3} \mu_{s} \right) \nabla \cdot u_{s} \right] I
$$
  
\n**Solid pressure,**  
\n
$$
P_{s} = \rho_{s} \varepsilon_{s} \theta + P_{s}^{C}
$$
  
\n**Collisional solid pressure,**  
\n
$$
P_{s}^{C} = 2\rho_{s} \varepsilon_{s}^{2} \theta_{g_{0}} (1 + e) \qquad \text{(Lun et al.)}
$$
  
\n**Particle shear viscosity,**  
\n
$$
\mu_{s} = \frac{4}{5} \varepsilon_{s}^{2} \rho_{s} d_{s} g_{0} (1 + e) \sqrt{\frac{\theta}{\pi}} + \mu_{s}^{K}
$$
  
\n**Particle kinetic viscosity,**  
\n
$$
\mu_{s}^{K} = \frac{10\rho_{s} d_{s} \sqrt{\pi \theta}}{96(1 + e)g_{0}} \left[ 1 + \frac{4}{5} (1 + e)g_{0} \varepsilon_{s} \right]^{2} \qquad \text{(Gidaspow et al.)}
$$
  
\n**Particle bulk viscosity,**  
\n
$$
\mu_{s} = \frac{4}{3} \varepsilon_{s}^{2} \rho_{s} d_{s} g_{0} (1 + e) \sqrt{\frac{\theta}{\pi}} \qquad \text{(Lun et al.)}
$$



Solid pressure,

 $\blacktriangleright$  11

### Frictional stress tensor – Schaeffer

$$
S_{s}^{f} = \left[ -P_{s}^{f} + \left( \xi_{s}^{f} - \frac{2}{3} \mu_{s}^{f} \right) \nabla \cdot u_{s} \right] I
$$
  
\nFrictional Solid pressure,  
\n
$$
P_{s}^{f} = 10^{25} (\varepsilon_{s} - \varepsilon_{s}^{\max})^{10} \qquad \varepsilon_{s} > \varepsilon_{s}^{\max}
$$
\n
$$
= 0 \qquad \varepsilon_{s} \leq \varepsilon_{s}^{\max}
$$
\nFrictional viscosity,  
\n
$$
\mu_{s}^{f} = \min \left( \frac{P_{s}^{f} \sin \phi}{\sqrt{4 I_{2D}}}, \mu_{s,\max}^{f} \right) \qquad \varepsilon_{s} > \varepsilon_{s}^{\max}
$$
\n
$$
= 0 \qquad \varepsilon_{s} \leq \varepsilon_{s}^{\max}
$$

$$
I_{2D} = \frac{1}{6} \Big[ (D_{s,11} - D_{s,22})^2 + (D_{s,22} - D_{s,33})^2 + (D_{s,33} - D_{s,11})^2 \Big] + D_{s,12}^2 + D_{s,23}^2 + D_{s,31}^2
$$

Particle bulk viscosity,  $\xi_s^f = 0$ 





#### Velocity vectors in transverse plane of drum for MD2





#### Velocity vectors in transverse plane of drum for PD2





#### Velocity vectors in transverse plane of drum for MD2





Stream wise velocity profile in transverse plane of drum along  $x = 0$ 







### Results – Active layer thickness





### Results – PD1





### Results – PD2





# Conclusions

- Qualitative trends in velocity profiles and void fraction distribution are captured
- Active layer thickness predicted reasonably well except for MD1
- Small difference between velocity profiles of polydispersed and mono-dispersed cases
- Small particles exist in core (3 mm), larger particles (5 and 6 mm) surround them while ones with 4 mm are spread across whole volume

